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MC/DC Masking



Masking MC/DC



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What is Masking MC/DC About?


- According to DO-178B, a condition is shown to independently affect the outcome of a decision by varying just that condition while holding fixed all other possible conditions
- Masking is an alternative approach to showing the independent effect of a condition on the outcome of a logical decision

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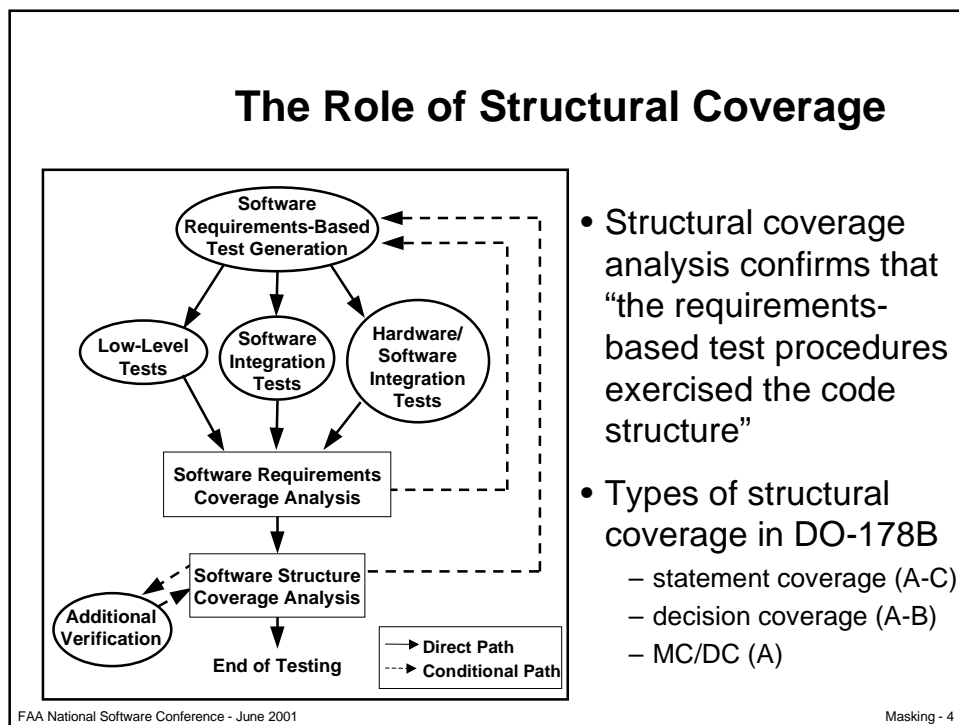
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Outline

- **Structural Coverage in the Context of DO-178B**
- **Modified Condition/Decision Coverage (MC/DC)**
 - what it is
 - what it isn't
- **Different Approaches to MC/DC**
 - Unique Cause vs. Masking
 - how are they different & how are they the same
 - for expressions with common logical operators
e.g., **A or B or C or D**; **A and B and C and D**
 - for expressions with mixed logical operators
e.g., **(A or B) and (C or D)**; **(A and B) or (C xor D)**

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Describing MC/DC

• MC/DC is

– based on the following criteria:

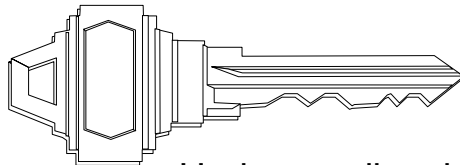
- ① every point of entry & exit in the program has been invoked at least once
- ② every condition in a decision in the program has taken all possible outcomes at least once
- ③ every decision in the program has taken all possible outcomes at least once
- ④ each condition in a decision has been shown to independently affect that decision's outcome

• MC/DC is *not*

- a testing method
- concerned with test cases developed from the source code (i.e., structural testing)
- guaranteed at the source code level if measured at the object code (and vice versa)
 - MC/DC can be demonstrated at the object code level *if* analysis demonstrates that coverage at the object code will be equivalent to the same coverage at the source code (FAQ 42, DO-248A)

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Understanding the implications of criteria ④ is the key to determining whether any approach (including masking) is acceptable for meeting the MC/DC objective

- What does independent effect mean?
 - Why do it?

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Independent Effect

- A condition independently affects a decision's outcome if that condition *alone* determines the outcome of the decision

a condition is shown to independently affect a decision's outcome by varying just that condition while holding fixed all other possible conditions



This tells you specifically HOW to show independent effect

- Chilenski/Miller defined specific minimum tests to demonstrate the independent effect of each condition at individual logical operators

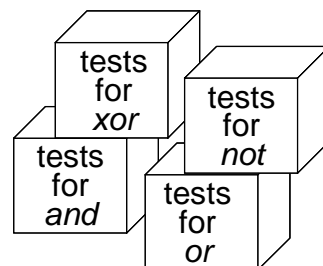
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Minimum Tests

- The minimum tests are intended to assure that each input to a logical operator correctly affects the outcome
- The minimum tests provide the building blocks for assessing MC/DC

logical operator = logical gate



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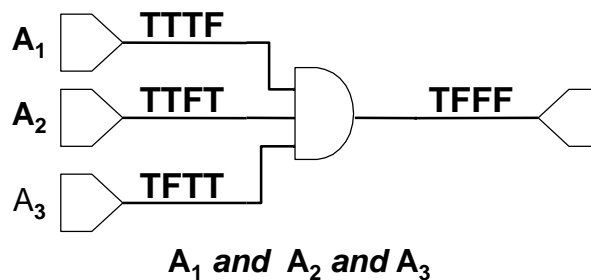
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Testing an n -input *and* Gate

A_1 and A_2 and A_3 and ... A_n

- Minimum testing to provide MC/DC requires
 - all inputs *true*, output *true*
 - each input individually *false*, output *false*
- Example: testing a 3-input *and* gate requires TTT, TTF, TFT, FTT



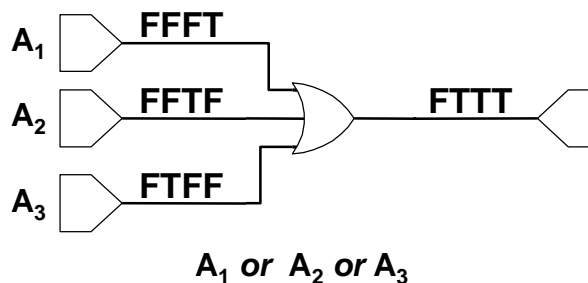
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Testing an n -input *or* Gate

A_1 or A_2 or ... A_n

- Minimum testing to provide MC/DC requires
 - all inputs *false*, output *false*
 - each input individually *true*, output *true*
- Example: testing a 3-input *or* gate requires FFF, FFT, FTF, TFF



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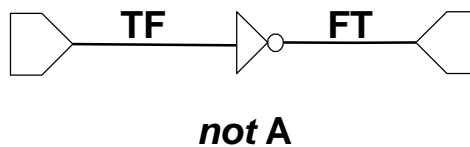
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Testing a *not* Gate

- **Minimum testing to provide MC/DC requires**
 - input *true*, output *false*
 - input *false*, output *true*
- **Example:**



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Testing an *xor* Gate

***xor* gates: are not like other gates**

- **More than one test set will satisfy the MC/DC criteria for an *xor* gate**
- **Minimum testing to provide MC/DC requires**
 - any of the following for a 2-input *xor*
 - TT, TF, FT
 - TF, FT, FF
 - FT, FF, TT
 - FF, TT, TF

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Controllability & Observability

- **Basic concepts of testing logic circuits:**
 - controllability: ability to control the inputs to a logical operator
 - observability: ability to observe the outputs of a logical operator at some end point
- **The minimum tests establish the inputs and expected outputs needed at a logical operator to show independent effect of each condition**

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Approaches to Independent Effect

- ***Unique cause* and *masking* are two approaches to showing the independent effect of a condition for multiple logical operators within a decision**
- **For expressions with common logical operators, unique cause and masking are the same**
 - for *A or B or C or D* or *A and B and C and D*
- **Differences emerge for expressions with mixed logical operators**
 - such as *(A or B) and (C or not D)*

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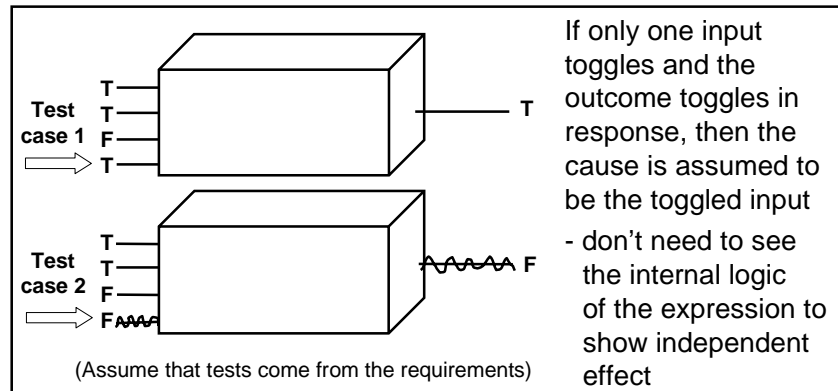
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Unique Cause

- A condition is shown to independently affect a decision's outcome by varying just that condition while holding fixed all other possible conditions



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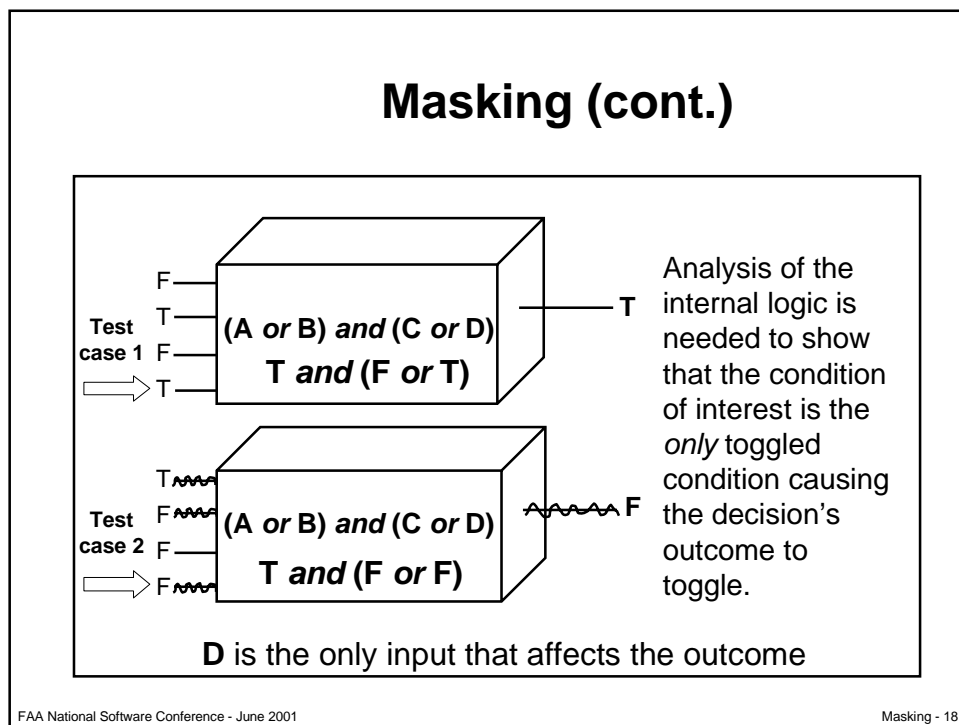
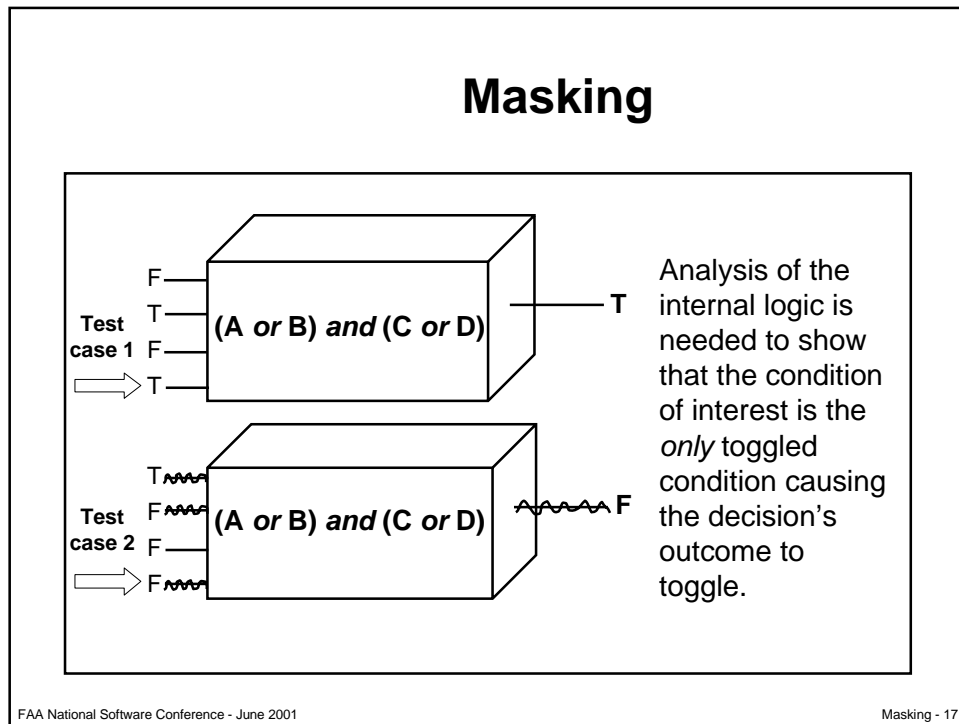
- A condition is shown to independently affect a decision's outcome using logic principles to assure that no other condition influences the outcome
 - even though more than one condition may change value
- Some inputs may hide or mask the effect of other inputs
 - *false and X* is always *false*
 - *true or X* is always *true*
- “Masking” principles are the converse
 - *true and X* is *X*
 - *false or X* is *X*

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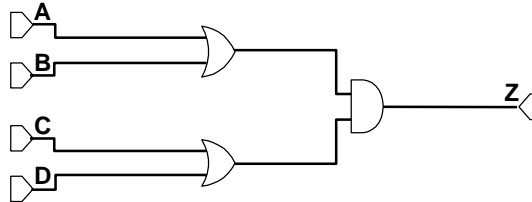


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Example $Z := (A \text{ or } B) \text{ and } (C \text{ or } D);$

Requirements:



Requirements-based test cases:

	1	2	3	4	5
A	F	F	T	T	F
B	F	T	F	F	T
C	T	T	T	F	F
D	F	F	F	F	T
Z	F	T	T	F	T

Do these test cases provide MC/DC of the source code?

Source code: $Z := (A \text{ or } B) \text{ and } (C \text{ or } D);$

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Truth Table Approach

$Z := (A \text{ or } B) \text{ and } (C \text{ or } D);$

A	B	C	D	Z
F	F	T	F	F
F	T	T	F	T
T	F	T	F	T
T	F	F	F	F
F	T	F	T	T

- Look for pairs of test cases where only one input value changes -- and the outcome changes
- There are no pairs of test cases where **D** is the only input value that changes

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Truth Table Approach

$Z := (A \text{ or } B) \text{ and } (C \text{ or } D);$

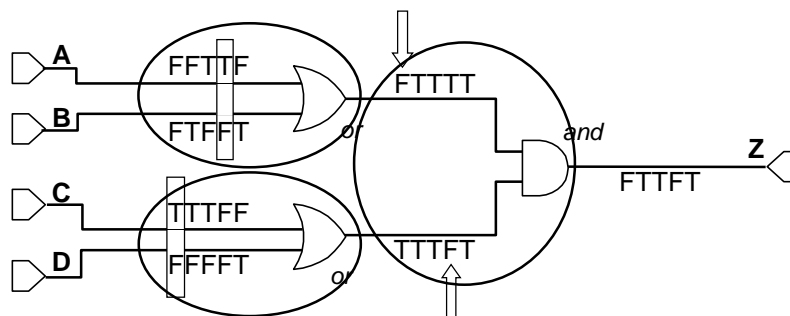
A	B	(A or B)	C	D	(C or D)	Z
F	F	F	T	F	T	F
F	T	T	T	F	T	T
T	F	T	T	F	T	T
T	F	T	F	F	F	F
F	T	T	F	T	T	T

- In these 2 test cases, **D** is the *only* condition that causes the outcome to change
 - these 2 cases show the independent effect of **D** -- even though more than one condition changes value

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Check for Minimum Tests



- Check for observability -- are the outputs of the or gates observable?
- Check for controllability -- do minimum tests exist for each logical gate?

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Analysis to confirm that you have the minimum tests is required for masking -- as opposed to simply showing independence pairs

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Coupled Conditions

One condition is coupled with another condition if the value of one condition influences the value of the other

- A test set for an expression with strongly coupled conditions *cannot* meet MC/DC using the unique cause approach
- A test set for an expression with coupled conditions *may* meet MC/DC using the masking approach

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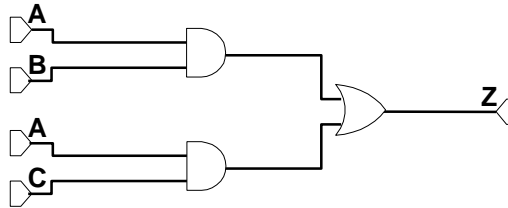
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Example $Z := (A \text{ and } B) \text{ or } (A \text{ and } C);$

Requirements:



Requirements-based test cases:

	1	2	3	4	5
A	T	F	T	T	F
B	T	T	F	F	F
C	F	F	F	T	T
Z	T	F	F	T	F

Do these test cases
provide MC/DC of the
source code?

Source Code: $Z := (A \text{ and } B) \text{ or } (A \text{ and } C);$

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Truth Table Approach

$Z := (A \text{ and } B) \text{ or } (A \text{ and } C);$

A	B		A	C		Z
T	T		T	F		T
F	T		F	F		F
T	F		T	F		F
T	F		T	T		T
F	F		F	T		F

- Expand the test cases to account for **A** being treated as 2 distinct conditions

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Truth Table Approach

Z := (A and B) or (A and C);

A	B	A and B	A	C	A and C	Z
T	T	T	T	F	F	T
F	T	F	F	F	F	F
T	F	F	T	F	F	F
T	F	F	T	T	T	T
F	F	F	F	T	F	F

- Expand the test cases to account for **A** being treated as 2 distinct conditions

⇒ Add the value of the subterms (**A and B**) and (**A and C**)

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Truth Table Approach

Z := (A and B) or (A and C);

A	B	A and B	A	C	A and C	Z
T	T	T	T	F	F	T
F	T	F	F	F	F	F
T	F	F	T	F	F	F
T	F	F	T	T	T	T
F	F	F	F	T	F	F

- Expand the test cases to account for **A** being treated as 2 distinct conditions
- Add the value of the subterms (**A and B**) and (**A and C**)

⇒ Check for independence pairs

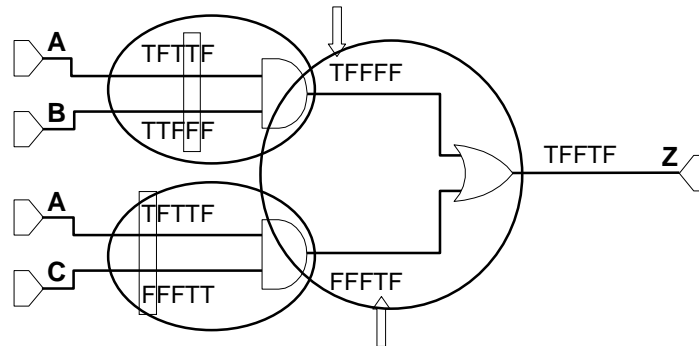
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Check for Minimum Tests



- Check for observability -- are the outputs of the *and* gates observable?
- Check for controllability -- do minimum tests exist for each logical gate?

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Pros and Cons of Masking

Pros

- Applies to more logic expressions than unique cause
 - because masking applies to expressions with coupled conditions
- Provides an additional check on the correctness of the source code
- Provides a practical approach for confirming MC/DC – both for manual and automated projects

Cons

- Requires analysis of the logic of each decision (this is not required for unique cause)
- Requires visibility into the logic of the source code

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Bottom Line

- You lose *nothing* using masking
 - *however*, the masking approach requires analysis of the logic of each expression (that is not required for unique cause) to confirm the independent effect of each condition
- You *gain* a method to handle expressions with coupled conditions

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Error Detection

Initial concern: masking would detect fewer errors than unique cause


- | | |
|--|--|
| <ul style="list-style-type: none">• For expressions with common logical operators<ul style="list-style-type: none">– there is no difference in error detection between unique cause and masking<ul style="list-style-type: none">• <i>because</i> there is no difference in the minimum test sets | <ul style="list-style-type: none">• For expressions with mixed logical operators<ul style="list-style-type: none">– no evidence exists of a practical difference in error detection between unique cause and masking– Chilenski's analysis of error sensitivity between unique cause and masking "has not shown that there is any significant difference." |
|--|--|

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Rationale for Accepting Masking

- **Does masking meet the definition of independent effect?**
 - Yes. Masking guarantees the same set of minimum tests at each logical operator (gate) as unique cause does
 - true for expressions with common logical operators
 - true for expressions with mixed logical operators
- **Does masking provide the same error detection capability?**
 - Yes. There is no evidence indicating any significant difference

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Acceptability of Masking MC/DC

Masking MC/DC meets the intent of the MC/DC objective

- **Certification Authorities Software Team (CAST) concurred that masking MC/DC should be an acceptable means of meeting the MC/DC objective**
 - at the February 2001 meeting
- **“Rationale for Accepting Masking MC/DC in Certification Projects” has been submitted for CAST approval**

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